# APPENDIX A: Sample Design For Pakistan Social And Living Standards Measurement Survey District Level, 2006-07

## **Objectives:**

The data generated though PSLM Survey will be used to assist the government in formulating the poverty reduction strategy as well as development plans at district level. The indicators will be developed at district level in the following sectors.

- 1. Education
- 2. Health
- 3. Water Supply & Sanitation.
- 4. Household Assets/Amenities.
- 5. Satisfaction to Service Delivery.

#### Universe:

The universe of this survey consists of all urban and rural areas of all four provinces, from the scope of the survey.

## **SAMPLING FRAME**

#### Urban area:

FBS has developed its own urban area frame. All urban areas comprising cities/towns have been divided into small compact areas known as enumeration blocks (E.Bs) identifiable through map. Each enumeration block comprises about 200-250 households and categorized into low, middle and high-income group, keeping in view the socio economic status of the majority of households. Urban area sampling frame consists of 26698 enumeration blocks has been updated in 2003.

#### Rural area:

With regard to the rural areas, the lists of villages/mouzas/dehs according to Population Census, 1998 have been used as sampling frame. In this frame, each village/mouza/deh is identifiable by its Name, Had Bast Number, Cadastral map etc. This frame is comprised 50590 villages/mouzas

The number of enumeration blocks in urban and mouzas/dehs/villages in rural areas of the country are as under:

NO. OF ENUMERATION BLOCKS AND VILLAGES AS PER SAMPLING FRAME

| Province      | Number of E. Blocks | Number of Villages |
|---------------|---------------------|--------------------|
|               |                     |                    |
| Punjab        | 14,549              | 25,875             |
| Sindh         | 9,025               | 5,871              |
| NWFP          | 1,913               | 7,337              |
| Balochistan   | 613                 | 6,557              |
| A.J.K         | 210                 | 1,654              |
| Northern Area | 64                  | 566                |
| FATA          |                     | 2,596              |
| Islamabad     | 324                 | 132                |
|               |                     |                    |
| Total         | 26,698              | 50,588             |

## STRATIFICATION PLAN

#### **Urban Areas**:

Within each district large sized cities having population five lacs and above have been treated as independent stratum. Each of these cities has further been sub-stratified into low, middle and high group's areas. The remaining cities/towns within each district have been grouped together to constitute an independent stratum.

#### **Rural Areas:**

The entire rural domain of a district for Punjab, Sindh, NWFP and Balochistan provinces has been considered as independent stratum.

## Sample Size and its Allocation:

To determine optimum sample size for this survey, analytical studies based on the results of Pakistan Demographic Survey, Labour Force and Pakistan Integrated Households Sample Survey were undertaken. Keeping in view the variability exist within the population for the characteristics for which estimates are to be prepared, population distribution, level of estimates and field resources available a sample size of 76520 households enumerated from 5348 sample PSUs (2262 from urban and 3086 from rural areas) has been considered sufficient to produce reliable estimates at district level in respect of all provinces. An Annexure-I showing sample sizes by districts in four provinces of Pakistan, is attached.

**Sample Design:** A two-stage stratified sample design has been adopted for this survey.

## **Selection of primary sampling Units (PSUs):**

Enumeration blocks in the urban domain and mouzas/dehs/villages in rural domain have been taken as primary sampling units (PSUs). In urban domain sample PSUs from each stratum have been selected by probability proportional to size (PPS) method of sampling scheme using households in each block as measure of size (MOS).

Similarly in rural areas, population of each village has taken as MOS for selection of sample villages using probability proportional to size method of selection.

# **Selection of Secondary Sampling Units (SSUs):**

Households within each sample Primary Sampling Unit (PSU) have been considered as Secondary Sampling Units (SSUs). 16 and 12 households have been selected from each sample village and enumeration block respectively by systematic sampling scheme with a random start.

## **Estimation Procedures:**

Detail of estimation procedures for estimates and their variances is attached as Annexure  $-\,\mathrm{II}$ .

District-Wise Distribution of Sample Areas  $\_Villages$  and Enumeration Blocks) and Household – PSLM 2006-07

|      | Districts       | Sam   | mple Area | as    | Sample Households |       |       |  |
|------|-----------------|-------|-----------|-------|-------------------|-------|-------|--|
| s.No |                 | Urban | Rural     | Total | Urban             | Rural | Total |  |
|      | PUNJAB          | 1086  | 1182      | 2268  | 12842             | 18840 | 31682 |  |
| 101. | Attock          | 15    | 27        | 42    | 175               | 426   | 601   |  |
| 102. | Rawalpindi      | 72    | 36        | 108   | 830               | 571   | 1401  |  |
| 103. | Jhelum          | 15    | 24        | 39    | 175               | 379   | 554   |  |
| 104. | Chakwal         | 15    | 27        | 42    | 179               | 429   | 608   |  |
| 105. | Sargodha        | 39    | 39        | 78    | 462               | 613   | 1075  |  |
| 106. | Bhakkar         | 15    | 24        | 39    | 179               | 383   | 562   |  |
| 107. | Khushab         | 15    | 21        | 36    | 180               | 335   | 515   |  |
| 108. | Mianwali        | 15    | 21        | 36    | 179               | 336   | 515   |  |
| 109. | Faisalabad      | 102   | 69        | 171   | 1221              | 1103  | 2324  |  |
| 110. | Jhang           | 27    | 54        | 81    | 321               | 863   | 1184  |  |
| 111. | T.T.Singh       | 21    | 33        | 54    | 251               | 526   | 777   |  |
| 112. | Gujranwala      | 57    | 36        | 93    | 677               | 573   | 1250  |  |
| 113. | Gujrat          | 22    | 33        | 55    | 257               | 522   | 779   |  |
| 114. | Sialkot         | 36    | 21        | 57    | 428               | 336   | 764   |  |
| 115. | Hafiza Abad     | 15    | 27        | 42    | 178               | 432   | 610   |  |
| 116. | Mandi Bahauddin | 15    | 27        | 42    | 179               | 432   | 611   |  |
| 117. | Narowal         | 15    | 30        | 45    | 180               | 480   | 660   |  |
| 118. | Lahore          | 208   | 27        | 235   | 2409              | 424   | 2833  |  |
| 119. | Kasur           | 27    | 42        | 69    | 319               | 665   | 984   |  |
| 120. | Okara           | 24    | 45        | 69    | 288               | 719   | 1007  |  |
| 121. | Sheikhupura     | 33    | 51        | 84    | 391               | 808   | 1199  |  |
| 122. | Vehari          | 19    | 42        | 61    | 227               | 672   | 899   |  |
| 123. | Sahiwal         | 15    | 36        | 51    | 180               | 576   | 756   |  |
| 124. | Multan          | 56    | 42        | 98    | 669               | 672   | 1341  |  |
| 125. | Khanewal        | 15    | 39        | 54    | 180               | 624   | 804   |  |
| 126. | Pakpattan       | 15    | 27        | 42    | 179               | 432   | 611   |  |
| 127. | Lodhran         | 15    | 21        | 36    | 180               | 335   | 515   |  |
| 128. | D.G.Khan        | 19    | 33        | 52    | 228               | 528   | 756   |  |
| 129. | Rajanpur        | 15    | 27        | 42    | 180               | 432   | 612   |  |
| 130. | Leiah           | 15    | 24        | 39    | 180               | 384   | 564   |  |
| 131. | Muzaffargarh    | 15    | 39        | 54    | 180               | 624   | 804   |  |
| 132. | Bahawalpur      | 39    | 42        | 81    | 461               | 671   | 1132  |  |
| 133. | Bahawalnagar    | 21    | 42        | 63    | 252               | 672   | 924   |  |
| 134. | R. Y. Khan      | 24    | 54        | 78    | 288               | 863   | 1151  |  |

| SINDH                    | 642        | 678        | 1320 | 7694 | 10838 | 18532 |
|--------------------------|------------|------------|------|------|-------|-------|
| 201. Khairpur            | 15         | 45         | 60   | 179  | 720   | 899   |
| 202. Sukkur              | 39         | 18         | 57   | 467  | 288   | 755   |
| 203. Nawab Shah          | 15         | 30         | 45   | 180  | 480   | 660   |
| 204. Neshero Feroz       | 15         | 36         | 51   | 180  | 576   | 756   |
| 205. Ghotki              | 15         | 36         | 51   | 180  | 576   | 756   |
| 206. Jacobabad           | 20         | 45         | 65   | 240  | 720   | 960   |
| 207. Shikarpur           | 15         | 30         | 45   | 180  | 480   | 660   |
| 208. Larkana             | 20         | 60         | 80   | 240  | 960   | 1200  |
| 209. <b>Dadu</b>         | 15         | 57         | 72   | 180  | 911   | 1091  |
| 210. Hyderabad           | 57         | 60         | 117  | 681  | 956   | 1637  |
| 211. Badin               | 15         | 42         | 57   | 177  | 670   | 847   |
| 212. Thatta              | 15         | 48         | 63   | 180  | 768   | 948   |
| 213. Sanghar             | 15         | 51         | 66   | 179  | 815   | 994   |
| 214. Mirpur Khas         | 21         | 54         | 75   | 252  | 862   | 1114  |
| 215. Tharparkar          | 12         | 39         | 51   | 144  | 624   | 768   |
| 216. DISTRICT OF KARACHI | 338        | 27         | 365  | 4055 | 432   | 4487  |
| N.W.F.P. TOTAL           | <u>258</u> | <u>591</u> | 849  | 3082 | 9443  | 12525 |
| 301. <b>SWAT</b>         | 12         | 27         | 39   | 144  | 432   | 576   |
| 302. UPPER DIR           | 5          | 26         | 31   | 59   | 416   | 475   |
| 303. LOWER DIR           | 6          | 27         | 33   | 72   | 432   | 504   |
| 304. CHITRAL             | 5          | 26         | 31   | 60   | 414   | 474   |
| 305. SHANGLA             | 0          | 27         | 27   | 0    | 432   | 432   |
| 306. MALAKAND            | 6          | 26         | 32   | 72   | 416   | 488   |
| 307. BONAIR              | 0          | 30         | 30   | 0    | 480   | 480   |
| 308. PESHAWAR            | 60         | 24         | 84   | 714  | 384   | 1098  |
| 309. CHARSADA            | 14         | 22         | 36   | 168  | 352   | 520   |
| 310. NOWSHERA            | 16         | 26         | 42   | 191  | 415   | 606   |
| 311. <b>KOHAT</b>        | 14         | 24         | 38   | 168  | 384   | 552   |
| 312. <b>KARK</b>         | 6          | 24         | 30   | 72   | 382   | 454   |
| 313. HANGU               | 8          | 21         | 29   | 96   | 335   | 431   |
| 314. <b>D.I.KHAN</b>     | 12         | 25         | 37   | 144  | 399   | 543   |
| 315. <b>TANK</b>         | 6          | 20         | 26   | 71   | 319   | 390   |
| 316. MANSEHRA            | 10         | 27         | 37   | 118  | 431   | 549   |
| 317. ABBOTABAD           | 16         | 21         | 37   | 190  | 336   | 526   |
| 318. BATAGRAM            | 0          | 27         | 27   | 0    | 431   | 431   |
| 319. KOHISTAN            | 0          | 25         | 25   | 0    | 400   | 400   |
| 320. HARIPUR             | 14         | 22         | 36   | 168  | 351   | 519   |
| 321. <b>BANNU</b>        | 8          | 22         | 30   | 95   | 351   | 446   |
| 322. LAKKI MARWAT        | 8          | 21         | 29   | 96   | 335   | 431   |
| 323. MARDAN              | 18         | 27         | 45   | 216  | 432   | 648   |
| 324. <b>SWABI</b>        | 14         | 24         | 38   | 168  | 384   | 552   |

| BALOCHISTAN TOTAL     | 195  | 521  | 716  | 2329  | 8325  | 10654 |
|-----------------------|------|------|------|-------|-------|-------|
| 401. QUETTA           | 45   | 21   | 66   | 533   | 334   | 867   |
| 402. PASHIN           | 5    | 20   | 25   | 60    | 320   | 380   |
| 403. QILLA ABDULLAH   | 8    | 20   | 28   | 95    | 320   | 415   |
| 404. CHAGHI           | 7    | 20   | 27   | 84    | 320   | 404   |
| 405. <b>SIBBI</b>     | 12   | 17   | 29   | 142   | 270   | 412   |
| 406. ZIARAT           | 2    | 20   | 22   | 24    | 320   | 344   |
| 407. <b>KOHLU</b>     | 2    | 20   | 22   | 24    | 320   | 344   |
| 408. DERA BUGTI       | 4    | 19   | 23   | 48    | 304   | 352   |
| 409. <b>KALAT</b>     | 6    | 20   | 26   | 72    | 319   | 391   |
| 410. MASTUNG          | 8    | 20   | 28   | 96    | 320   | 416   |
| 411. KHUZDAR          | 11   | 20   | 31   | 132   | 320   | 452   |
| 412. AWARAN           | 0    | 20   | 20   | 0     | 320   | 320   |
| 413. KHARAN           | 5    | 20   | 25   | 60    | 320   | 380   |
| 414. LASBILLA         | 12   | 20   | 32   | 144   | 320   | 464   |
| 415. KETCH/TURBAT     | 8    | 22   | 30   | 96    | 352   | 448   |
| 416. GWADAR           | 12   | 14   | 26   | 144   | 224   | 368   |
| 417. PANJGUR          | 5    | 21   | 26   | 60    | 336   | 396   |
| 418. <b>ZHOB</b>      | 8    | 21   | 29   | 96    | 336   | 432   |
| 419. LORALAI          | 6    | 21   | 27   | 72    | 336   | 408   |
| 420. BARKHAN          | 2    | 20   | 22   | 24    | 320   | 344   |
| 421. MUSA KHEL        | 0    | 22   | 22   | 0     | 352   | 352   |
| 422. QILLAH SIAFULLAH | 4    | 22   | 26   | 48    | 352   | 400   |
| 423. NASIRABAD        | 6    | 21   | 27   | 72    | 336   | 408   |
| 424. JAFARABAD        | 8    | 20   | 28   | 96    | 320   | 416   |
| 425. JHAL MAGSI       | 2    | 20   | 22   | 23    | 318   | 341   |
| 426. BOLAN/KACHHI     | 7    | 20   | 27   | 84    | 316   | 400   |
| 1. ISLAMABAD          | 30   | 15   | 45   | 326   | 234   | 560   |
| PAKISTAN              | 2211 | 2987 | 5198 | 26273 | 47680 | 73953 |

# **Estimation Procedure:**

## ESTIMATION PROCEDURE ADOPTED FOR PSLM SURVEY

#### **NOTATIONS:**

N<sub>h</sub> = Total number of Primary Sampling Units (PSUs) in the hth stratum of a province.

 $n_h\,$  = Total number of sample PSUs in the hth stratum of a province.

 $M_{hi}$  = Total number of Secondary Sampling Units (SSUs) in the ith sample PSU of hth stratum of a province.

 $m_{hi}$  = Number of sample SSUs in the ith sample PSU of hth stratum of a province.

P<sub>hi</sub> = Assigned probability of selection of ith PSU of the hth stratum of a province.

 $y_{hij}$  = Value of any characteristic y of jth SSU within ith PSU of hth stratum of a province.

 $x_{hij}$  = Value of any characteristic x of jth SSU within ithPSU of hth stratum of a province with whose respect proportion is required.

## (i): ESTIMATION FORMULAE FOR TOTALS AND THEIR VARIANCES

$$N = \sum_{h=1}^{L} N_h$$

$$n = \sum_{h=1}^{L} n_h$$

$$\vec{Y}_h = \frac{1}{n_h} \sum_{i=1}^{n_h} \frac{\vec{Y}_{hi}}{p_{hi}}$$

OR

$$\vec{P}_{h} = \frac{1}{n_{h}} \sum_{i=1}^{n_{h}} \frac{1}{p_{hi}} \frac{M_{hi}}{m_{hi}} \sum_{i=1}^{m_{hi}} y_{hij}$$

$$\vec{Y} = \sum_{h=1}^{L} \vec{Y}_{h} = \sum_{h=1}^{L} \frac{1}{n_{h}} \sum_{i=1}^{n_{h}} \frac{\vec{Y}_{hi}}{p_{hi}}$$

For X, another variable of interest, we have

$$\vec{X}_{h} = \frac{1}{n_{h}} \sum_{i=1}^{n_{h}} \frac{\vec{X}_{hi}}{P_{hi}} = \frac{1}{n_{h}} \sum_{i=1}^{n_{h}} \frac{1}{P_{hi}} \frac{M_{hi}}{m_{hi}} \sum_{j=1}^{m_{hi}} x_{hij}$$

$$\vec{X} = \sum_{h=1}^{L} \vec{X}_{h} = \sum_{h=1}^{L} \frac{1}{n_{h}} \sum_{i=1}^{n_{h}} \frac{\vec{X}_{hi}}{P_{hi}}$$

$$\vec{R} = \frac{\vec{Y}}{\vec{X}_{hi}}$$

$$v(\vec{y}_{h}) = \frac{1}{n_{h}} s^{2}_{ht} = \frac{1}{n_{h}(n_{h} - 1)} \left[ \sum_{i=1}^{n_{h}} \frac{\vec{Y}^{2}_{hi}}{P^{2}_{hi}} - \frac{(\sum_{i=1}^{n_{h}} \frac{\vec{y}_{hi}}{P_{hi}})^{2}}{n_{h}} \right]$$
$$v(\vec{Y}) = \sum_{h=1}^{L} \frac{1}{n_{h}} s^{2}_{ht} = \sum_{h=1}^{L} \frac{1}{n_{h}(n_{h} - 1)} \left[ \sum_{i=1}^{n_{h}} \frac{\vec{Y}^{2}_{hi}}{P^{2}_{hi}} - \frac{(\sum_{i=1}^{n_{h}} \frac{\vec{y}_{hi}}{P_{hi}})^{2}}{n_{h}} \right]$$

## (ii): FORMULA FOR RATIO ESTIMATES

$$r = \frac{\vec{y}}{\vec{X}}$$

where Y<sup>^</sup> and X<sup>^</sup> can be estimated by equations under item (i) given above.

$$Rel\ V(r) = \frac{1}{\vec{X}^{2}} \sum_{h=1}^{L} \frac{1}{n_{h}} s^{2}_{hb} + \frac{1}{\vec{x}^{2}} \sum_{h=1}^{L} \frac{1}{n_{h}} \sum_{i=1}^{n_{h}} \frac{M^{2}_{hi}}{p^{2}_{hi} m_{hi}} \frac{\left(M_{hi} - m_{hi}\right)}{M_{hi}} s^{2}_{hw}$$

where

$$s_{hb}^{2} = s_{ht}^{2} - s_{hw}^{2}$$

$$s_{ht}^{2} = s_{hy}^{2} + r_{shy}^{2} - 2r_{shxy}$$

$$s_{hx}^{2} = \frac{1}{(n_{h} - 1)} \left[ \sum_{i=1}^{n_{h}} \frac{\hat{x}_{hi}^{2}}{p_{hi}^{2}} - \frac{\left(\sum_{i=1}^{n_{h}} \frac{\hat{x}_{hi}}{p_{hi}}\right)^{2}}{n_{h}} \right]$$

$$s^{2}_{hy} = \frac{1}{(n_{h}-1)} \left[ \sum_{i=1}^{n_{h}} \frac{\vec{y}^{2}_{hi}}{p^{2}_{hi}} - \frac{\left(\sum_{i=1}^{n_{h}} \vec{y}_{hi}\right)^{2}}{n_{h}} \right]$$

$$s_{hxy} = \frac{1}{n_{h}-1} \left[ \sum_{i=1}^{n_{h}} \left( \frac{\vec{X}_{hi}}{p_{hi}} \frac{\vec{y}_{hi}}{p_{hi}} \right) - \frac{\left(\sum_{i=1}^{n_{h}} \frac{\vec{X}_{hi}}{p_{hi}}\right) \left(\sum_{i=1}^{n_{h}} \frac{\vec{y}_{hi}}{p_{hi}}\right)}{n_{h}} \right]$$

$$s_{hw}^{2} = \frac{1}{n_{h}-1} \sum_{i=1}^{n_{h}} \frac{1}{p_{hi}^{2}} \frac{M_{hi}^{2} (M_{hi} - m_{hi})}{m_{hi}} s_{hi}^{2}$$

and

$$s_{hi}^2 = s_{hiy}^2 + r_{S_{hix}}^2 - 2r_{S_{hixy}}$$

$$s^{2}_{hiy} = \frac{1}{(m_{hi}-1)} \left[ \sum_{j=1}^{m_{hi}} y^{2}_{hij} - \frac{\left(\sum_{j=1}^{m_{hi}} y_{hij}\right)^{2}}{m_{hi}} \right]$$

$$s^{2}_{hix} = \frac{1}{(m_{hi} - 1)} \left[ \sum_{j=1}^{m_{hi}} x^{2}_{hij} - \frac{\left(\sum_{j=1}^{m_{hi}} x_{hij}\right)^{2}}{m_{hi}} \right]$$

$$s^{2}_{hixy} = \frac{1}{(m_{hi}-1)} \left| \sum_{j=1}^{m_{hi}} x_{hij} y_{hij} - \frac{\left(\sum_{j=1}^{m_{hi}} x_{hij} \sum_{j=1}^{m_{hi}} y_{hij}\right)}{m_{hi}} \right|$$